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A robust constraint on the temperature and height of the extratropical tropopause

David W. J. Thompson^{1, 2}, Paulo Ceppi³, Ying Li²

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¹ Corresponding author. Email: davet@atmos.colostate.edu
² Department of Atmospheric Science, Colorado State University, Fort Collins, CO., USA
³ Grantham Institute for Climate Change and the Environment, Imperial College London, London, UK

1 **Abstract**

2 In a recent study, the authors hypothesize that the Clausius-Clapeyron relation provides a
3 strong constraint on the temperature of the extratropical tropopause, and hence the depth of mixing
4 by extratropical eddies. The hypothesis is a generalization of the fixed-anvil temperature hypothesis
5 to the global atmospheric circulation. It posits that the depth of robust mixing by extratropical
6 eddies is limited by radiative cooling by water vapor - and hence saturation vapor pressures - in areas
7 of sinking motion. The hypothesis implies that: 1) radiative cooling by water vapor constrains the
8 vertical structure and amplitude of extratropical dynamics and 2) the extratropical tropopause should
9 remain at roughly the same temperature and lift under global warming.

10 Here the authors test the hypothesis in numerical simulations run on an aquaplanet general
11 circulation model (GCM) and a coupled atmosphere-ocean GCM (AOGCM). The extratropical
12 cloud top height, wave driving, and lapse-rate tropopause all shift upwards but remain at roughly the
13 same temperature when the aquaplanet GCM is forced by uniform surface warming of +4K, and
14 when the AOGCM is forced by RCP8.5 scenario emissions. “Locking” simulations run on the
15 aquaplanet GCM further reveal that: 1) Holding the water vapor concentrations input into the
16 radiation code fixed while increasing surface temperatures strongly constrains the rise in the
17 extratropical tropopause whereas 2) increasing the water vapor concentrations input into the
18 radiation code while holding surface temperatures fixed leads to robust rises in the extratropical
19 tropopause.

20 Together, the results suggest that roughly invariant extratropical tropopause temperatures
21 constitutes an additional “robust response” of the climate system to global warming.

22

1 **1. Introduction**

2 In a recent paper (Thompson et al. 2017), we hypothesized that clear-sky radiative cooling by
3 water vapor plays a key role in governing the vertical extent of large-scale mixing by extratropical
4 eddies and thus of the depth of the extratropical troposphere. The hypothesis implies that the
5 extratropical tropopause should stay at roughly the same temperature under global warming, and
6 thus provides an explanation for why the tropopause lifts under climate change (e.g., Mitchell and
7 Ingram 1992; Santer et al. 2003; Lorenz and DeWeaver 2007; Singh and O’Gorman 2012). It also
8 provides a physical explanation for why the climate feedbacks associated with high clouds in the
9 tropics (Hartmann and Larson 2002; Zelinka and Hartmann 2010) also appear in association with
10 clouds in the extratropics (e.g., Wetherald and Manabe 1988; Zelinka et al. 2012, 2013). In this paper
11 we test the hypothesis outlined in Thompson et al. (2017) in a series of numerical experiments. We
12 begin with a brief review of the underlying physics.

13

14 *Physical basis*

15 At steady-state and on large (i.e., quasi-geostrophic) scales, the transformed Eulerian mean
16 (TEM) thermodynamic energy and zonal momentum equations can be expressed as:

17

$$18 \quad 1) \quad \overline{f\bar{v}^*} = -\nabla \cdot \bar{F}$$

19

$$20 \quad 2) \quad -\overline{\bar{\omega}^* S} = \bar{Q}$$

21

22 where the overbars denote zonal averages, \bar{v}^* and $\bar{\omega}^*$ denote the zonal-mean residual circulation,
23 $\nabla \cdot \bar{F}$ denotes the divergence of the Eliassen-Palm (EP) flux (i.e., the “wave driving” of the large-

1 scale circulation), and \bar{Q} denotes diabatic processes. The EP flux divergence reflects the effects of
2 wave drag on the zonal-mean flow and - on QG scales - is equivalent to the eddy flux of potential
3 vorticity: Regions of negative EP flux divergence (i.e., EP flux convergence) correspond to regions
4 where the eddy flux of PV is equatorward, and vice versa. By construction, the residual circulation
5 corresponds to the component of the circulation that balances diabatic heating and thus
6 approximates the diabatic (i.e., cross-isentropic) mass flux. In regions where $\bar{\omega}^*$ is downward, there
7 must be an imbalance between the zonal-mean diabatic heating (due to, say, condensational heating)
8 and the zonal-mean diabatic cooling (due to, say, clear-sky radiative cooling). The residual zonal-
9 mean diabatic cooling presumably derives from clear-sky radiative cooling.

10 The largest values of climatological-mean EP flux convergence (and thus equatorward eddy
11 fluxes of PV) are located near the level of the midlatitude extratropical tropopause (Fig. 1, shading).
12 The resulting westward torque is balanced by the Coriolis acceleration acting on poleward residual
13 motion in the midlatitude upper troposphere (Eq. 1; Fig. 1, contours). The poleward motion is, in
14 turn, accompanied by downward motion in the mid-high latitude troposphere, and the downward
15 motion at high latitudes is balanced by atmospheric radiative cooling (Eq. 2).

16 The linkages between the EP flux divergence, the overturning residual circulation, and
17 radiative cooling are generally viewed in the context of forcing by the wave drag: The larger the wave
18 drag, the larger the amplitude of the residual circulation and thus of the dynamical heating and
19 radiative cooling at high latitudes. From this perspective, the depth of the region of largest mixing in
20 the extratropics - i.e., the depth of the extratropical troposphere - is constrained by the dynamics of
21 baroclinic instability (the “dynamical constraint”; Held 1982; Schneider 2004). The results in
22 Thompson et al. (2017) suggest that the depth of vigorous mixing in the extratropics is also
23 constrained by the vertical structure of clear-sky radiative cooling. The reasoning is as follows.

24 In sinking regions of the atmosphere, Q (Eq. 2) is dominated by water vapor radiative

1 cooling (Simpson 1928; Manabe and Strickler 1964; Ingram 2010). The radiative cooling decreases
2 sharply in the upper tropical troposphere at temperatures where the saturation vapor pressure - and
3 hence the amount of water vapor available for radiant emissions - becomes very small in accordance
4 with the Clausius-Clapeyron relation (Manabe and Strickler 1964; Hartmann et al. 2001). If clear-sky
5 radiative cooling constrains the residual vertical motion $\bar{\omega}^*$, then from continuity it must also
6 constrain \bar{v}^* . And if clear-sky radiative cooling constrains \bar{v}^* , it must also constrain the amplitude
7 of tropospheric wave breaking $-\nabla \cdot \mathbf{F}$. From this perspective, the amplitude of tropospheric wave
8 breaking and thus tropospheric diabatic mixing can only be as large as clear-sky radiative cooling will
9 allow.

10

11 *Motivation*

12 The hypothesis outlined in Thompson et al. (2017) is a generalization of the physics of the
13 “fixed anvil temperature (FAT)” hypothesis to large-scale extratropical dynamics: The FAT
14 hypothesis posits that the temperature of tropical anvil clouds is constrained by the amplitude of
15 clear-sky radiative cooling by water vapor (Hartmann and Larson 2002); Thompson et al (2017)
16 argue that the same basic physics should also constrain the depth of large-scale diabatic mixing by
17 extratropical eddies and thus of extratropical tropopause height. The generalization of the FAT
18 hypothesis to the extratropical circulation has three primary implications: 1) It suggests that the
19 depth of the extratropical troposphere is constrained by water vapor radiative cooling and thus the
20 thermodynamic properties of water vapor; 2) it predicts that the extratropical tropopause should
21 remain at roughly the same temperature under global warming, and thus provides a physical
22 explanation for the lifting of the extratropical circulation in climate change simulations (e.g., Mitchell
23 and Ingram 1992; Santer et al. 2003; Lorenz and DeWeaver 2007; Singh and O’Gorman 2012); and
24 3) it provides a physical explanation for the positive cloud feedbacks found at extratropical latitudes

1 (e.g., Wetherald and Manabe 1988; Zelinka et al. 2012, 2013).

2 Here we test the generalization of the FAT hypothesis to the extratropical circulation in
3 experiments run on an aquaplanet general circulation model (GCM) and in output from a coupled
4 atmosphere/ocean GCM (AOGCM). Section 2 describes the numerical experiments; Section 3
5 presents results based on the aquaplanet experiments; and Section 4 presents results based on the
6 coupled AOGCM. Conclusions are given in Section 5.

7 8 **2. Numerical experiments and datas**

9 *Aquaplanet experiments*

10 The aquaplanet experiments were run on the National Center for Atmospheric Research
11 (NCAR) Community Atmospheric Model Version 4 (CAM4). The version used here has a
12 horizontal resolution of 1.9° latitude by 2.5° longitude, includes 26 vertical levels spanning the
13 surface to 3.54 hPa, and explicitly calculates the shortwave and longwave radiative fluxes as per
14 Collins et al. (2006). All experiments were run for five years (with the first year omitted to account
15 for spinup) with specified sea-surface temperatures (SSTs) under perpetual equinox conditions, and
16 there is no land/sea geometry. Since the model is equatorially symmetric, the results are averaged
17 over both hemispheres to increase the sample size in the analyses.

18 The effects of water vapor radiative cooling on the atmospheric circulation are explored in
19 three primary sets of experiments run on the aquaplanet GCM. In Set 1, we test whether
20 extratropical clouds, extratropical wave-drag, and the extratropical tropopause rise and remain at
21 roughly the same temperature in simulations where SSTs are raised uniformly by 4 K. In Sets 2 and
22 3, we explore the role of water vapor radiative cooling on the circulation in two locking experiments:
23 In Set 2, SSTs are increased uniformly by 4 K but the water vapor concentrations input into the
24 radiation code are held fixed at their control values; in Set 3, SSTs are held fixed at their control

1 values but the water vapor concentrations input into the radiation code are increased to the values
2 derived from the warming experiment in Set 1. Experiments similar to the latter were performed in
3 Harrop and Hartmann (2012), but were focused on tropical anvil clouds in a cloud-resolving model.
4 Here we explore the effects of water vapor radiative cooling on the global-scale circulation in an
5 aquaplanet GCM.

6 The details of the experiments are as follows:

7 • The T_{at} simulation was forced with the idealized, equatorially symmetric “Qobs” SST profile
8 specified in Neale and Hoskins 2000 (the same configuration used in the CFMIP aquaplanet
9 experiments).

10 • The T_{+4K} simulation is identical to the T_{at} simulation, except that SSTs are raised by 4 K
11 relative to their control values.

12 • The $T_{at}W_{at}$ “locking” experiment was forced: 1) with the SST profile from the T_{at} experiment
13 and 2) by overwriting the water vapor concentrations input into the radiation code at each radiative
14 time step with resampled instantaneous values of the water vapor concentrations output from the T_{at}
15 experiment. The water vapor concentrations were resampled by shifting the values by one year so
16 that the resampled water vapor values 1) are decoupled from the values calculated by the model 2)
17 have the same long-term mean, autocorrelation and variance as the original values.

18 The effects of the locking methodology on the model atmosphere can be estimated by
19 comparing the $T_{at}W_{at}$ and T_{at} simulations. Decoupling the water vapor concentrations input into the
20 radiation code from those calculated by the model means that the radiation scheme in the $T_{at}W_{at}$
21 simulation may “see” dry air in a moist updraft, and vice versa. It also means that the water vapor
22 concentrations input into the radiation code may exceed the saturation vapor pressure. In practice,
23 the locking methodology leads to a weak cooling of the polar lower stratosphere but otherwise does
24 not notably influence mean atmospheric temperatures (not shown).

1 • The $T_{+4K}W_{at}$ and $T_{at}W_{+4K}$ “locking” experiments are run in an analogous manner to the $T_{at}W_{at}$
2 experiment. In the $T_{+4K}W_{at}$ experiment, SSTs are set to their T_{+4K} simulation values while the water
3 vapor concentrations input into the radiation code are set to their (resampled) T_{at} simulation values.
4 In the $T_{at}W_{+4K}$ experiment, SSTs are set to their T_{at} simulation values while the water vapor
5 concentrations input into the radiation code are set to their (resampled) T_{+4K} simulation values.

6 7 *AOGCM output*

8 The hypotheses are also explored in numerical output from the Institute Pierre- Simon
9 Laplace (IPSL) climate model (version IPSL-CM5A-LR; Dufresne et al. 2013). We use two runs that
10 were conducted under the auspices of the Coupled Model Intercomparison Project phase 5
11 (CMIP5): 1) years 1979–2005 from the “historical” run (i.e., the run forced with estimates of
12 historical anthropogenic forcing) and 2) years 2070–2099 from the Representative Concentration
13 Pathway (RCP) 8.5 scenario run (i.e., the run forced with the RCP8.5 future anthropogenic forcing).
14 The differences between the two runs represent the circulation response to 21st century forcing.
15 The IPSL model output is available on a 3.75 latitude \times 1.875 longitude mesh and at 39 vertical
16 levels. Details of the physics parameterizations used in the IPSL AGCM are provided in Hourdin et
17 al. (2006).

18 19 *Observations*

20 The observational analyses shown in Figure 1 are derived the ECMWF Interim Reanalysis
21 ERA-Interim output sampled at 6 hourly intervals (Dee et al. 2011).

22 23 *Analysis details*

24 The EP flux divergence and transformed Eulerian mean (TEM) circulation are calculated in

1 spherical coordinates using the quasi-geostrophic form of the equations (Edmon et al. 1980). Cloud
 2 top pressure is defined as the level where cloud fraction decreases to 0.01 (note that this definition
 3 does not necessary link directly to the radiative emission temperature of the cloud). The lapse-rate
 4 tropopause is defined as the lowest level where the lapse rate decreases below 2 K/km, and remains
 5 below 2 K/km within the overlying 2km of the atmosphere. The clear-sky mass flux is defined as
 6 the flux required to balance the net diabatic cooling in clear-sky regions of the model, and is
 7 calculated as

8

9 3)
$$\omega_{clear} \equiv -\frac{Q_{clear}}{S_{clear}},$$

10

11 where Q_{clear} and S_{clear} are the radiative cooling and static stability in clear-sky regions, respectively
 12 (the atmospheric radiative cooling includes both shortwave and longwave components, but is
 13 dominated by the latter).

14

15 **3. Response of the extratropical tropopause to variations in surface temperature and**
 16 **atmospheric radiative cooling**

17 In this section, we explore the circulation response in three sets of experiments:

18 *Experiment Set 1): The differences between the T_{+4K} and T_{at} simulations.*

19 The T_{+4K} and T_{at} simulations differ only in the SSTs prescribed as the lower boundary
 20 condition, thus the differences between the two allow us to test whether the extratropical
 21 tropopause (and thus mixing by large-scale extratropical variability) lifts globally in a manner
 22 predicted by the physics outlined in the Introduction.

23 *Experiment Sets 2 and 3): The differences between the $T_{+4K}W_{at}$ and $T_{at}W_{at}$ simulations (Set 2) and between*

1 *the $T_{at}W_{+4K}$ and $T_{at}W_{at}$ simulations (Set 3).*

2 The $T_{+4K}W_{at}$ and $T_{at}W_{+4K}$ “locking” experiments isolate the role of water vapor radiative
3 cooling in the circulation response to surface warming in two different frameworks: One in which
4 the water vapor concentrations input into the radiation code are held fixed while SSTs are increased
5 ($T_{+4K}W_{at}$); and one in which the water vapor concentrations input into the radiation code are
6 increased while SSTs are held fixed ($T_{at}W_{+4K}$).

7
8 *Experiment Set 1: The circulation response to surface warming in an aquaplanet GCM*

9 The left column in Figure 2 shows the long-term mean, (a) zonal-mean temperature and (c)
10 specific humidity from the T_{at} simulation. Temperatures decrease with both latitude and altitude
11 throughout the atmosphere from peak values in the tropical troposphere. The temperature
12 minimum in the tropical stratosphere arises from the model Brewer-Dobson circulation which - as
13 expected due to the lack of orography in the model - is weaker than the observed. To first order, the
14 latitude/height structure of the model specific humidity mirrors that of tropospheric temperatures,
15 as mandated by the physics expressed in the Clausius-Clapeyron relation. The 220 K isotherm and
16 0.5 g/kg isopleth are both located at ~ 200 hPa in the tropics and ~ 400 hPa at high latitudes (black
17 contours).

18 The right column shows the differences in zonal-mean temperature and specific humidity
19 between the T_{+4K} and T_{at} simulations. As expected, raising SSTs by 4 K leads to widespread warming
20 throughout the model troposphere and thus increases in specific humidity (shading). The warming
21 peaks in the model tropical troposphere (panel b), where temperatures are closely fixed to the moist
22 adiabatic lapse rate. The increases in surface temperature lead to a ~ 30 -50 hPa lifting of the 220 K
23 and 0.5 g/kg isopleths (black contours).

24 Figure 3 shows corresponding results for clear-sky radiative cooling, the clear-sky mass flux

1 divergence (recall that the clear-sky mass flux is defined in Eq. 3), cloud fraction, and the EP flux
2 divergence. The left column shows results from the T_{at} simulation; the right column shows the
3 differences between the T_{+4K} and T_{at} simulations. In the control simulation, the clear-sky cooling
4 peaks in the tropical troposphere and decreases with both altitude and latitude (Fig. 3a), consistent
5 with the meridional structure of specific humidity (Fig. 2c). The clear-sky mass fluxes likewise
6 decrease rapidly with altitude - and thus the mass flux divergences have largest amplitude in the
7 model upper troposphere (Fig. 3c). Cloud fraction decreases rapidly with height in the vicinity of the
8 maximum in the clear-sky mass flux divergence (shading in Fig. 3e), and cloud top extends to just
9 below 100 hPa in the tropics and ~ 200 hPa at high latitudes (the contour in Fig. 3e indicates the
10 0.07 cloud fraction isopleth). The EP flux convergence is largest - i.e., the torque due to wave drag is
11 largest westward - in the upper extratropical troposphere between ~ 300 -500 hPa (Fig. 3g).

12 Increasing SSTs by 4 K leads to widespread increases in clear-sky radiative cooling in the
13 upper troposphere (Fig. 3b). The changes in clear-sky cooling rates are weaker in the middle
14 troposphere than they are near the tropopause (Fig. 3b; shading), presumably because the water
15 vapor absorption bands are already opaque to terrestrial radiation in the T_{at} simulation. The increases
16 in clear-sky radiative cooling lead to a lifting of the level where the clear-sky radiative cooling
17 decreases rapidly with height (Fig. 3b; contours) and thus also in the levels of largest clear-sky
18 flux divergences (Fig. 3d). Importantly, the upward shifts in the levels of vanishing clear-sky
19 radiative cooling and largest mass flux divergences are not limited to the tropics, but span the
20 extratropics as well.

21 Consistent with the physics outlined in the Introduction, raising SSTs by 4 K also leads to a
22 lifting of the vertical profiles of cloud fraction and EP flux divergence. The vertical shifts in both
23 fields are evidenced as vertical dipoles in the differences: Cloud fraction generally increases in the
24 upper troposphere but decreases in the lower troposphere; the EP flux convergence shifts upward

1 and poleward, consistent with both a lifting and poleward shift of the model stormtrack (i.e., see the
2 isopleths in Fig. 3h). Throughout most of the globe, cloud top and the level of largest negative EP
3 flux divergences both lift by roughly the same distance as the clear-mass flux divergences do
4 (contours in Figs. 3f and 3h). The most notable exception is the large rises in cloud top over very
5 high latitudes.

6 Figure 4 summarizes the response of the extratropical tropospheric circulation to surface
7 warming in pressure (left) and temperature (right) coordinates. As noted above, increasing surface
8 temperatures by 4 K leads to a rising of the 220 K isotherm by ~ 30 -50 hPa at all latitudes (solid lines
9 in all left panels). As the upper troposphere warms, the level of largest mass flux divergences rises
10 (dotted lines in Fig. 4a). And as the clear-sky mass flux divergences rise, so does cloud-top (dotted
11 lines in Fig. 4c), the level of largest negative EP-flux divergence (dotted lines in Fig. 4e), and the
12 lapse rate extratropical tropopause (dotted lines in Fig. 4g). The temperature of all four fields stays
13 relatively invariant, particularly at extratropical latitudes, despite the fact that the upper troposphere
14 is warming substantially (right column). The relatively weak lifting of the lapse-rate tropopause and
15 cloud top at tropical latitudes (panels 4c and 4g) is consistent with the adjustment of the clear-sky
16 mass fluxes to the increases in static stability as tropical temperatures shift to a warmer moist adiabat
17 (Zelinka and Hartmann 2010).

18
19 *Experiment Sets 2 and 3: Isolating the role of water vapor radiative cooling in the circulation response to surface*
20 *warming*

21 Experiment Sets 2 and 3 explore the effects of water vapor radiative cooling on the
22 circulation response to surface warming in the $T_{+4K}W_{cl}$ and $T_{cl}W_{+4K}$ “locking” experiments. The left
23 column in Fig. 5 is reproduced from the right panels of Figs. 2 and 3, and recaps the *total* response
24 to increasing SSTs by 4 K. As discussed in the previous section, the response is characterized by

1 temperature and specific humidity increases in the troposphere (Fig. 5a, d), temperature decreases in
2 the stratosphere (Fig. 5a), enhanced long-wave cooling in the upper troposphere (Fig. 5g), and an
3 upward shift of the regions of largest clear-sky mass flux divergence (Fig. 5j), cloud fraction (Fig.
4 5m), EP flux divergence (Fig. 5p) and the lapse rate tropopause (Fig. 4g).

5 The middle column in Fig. 5 ($T_{+4K}W_{at}$ minus $T_{at}W_{at}$) shows the response to increasing SSTs by
6 +4K while locking the water vapor concentrations input into the radiation code at their control
7 values. Note that 1) the specific humidities seen by the radiation code in both the $T_{+4K}W_{at}$ and $T_{at}W_{at}$
8 simulations are identical and are indicated in Fig. 2c, and 2) the differences between the specific
9 humidities seen by everything *but* the radiation code in the $T_{+4K}W_{at}$ and $T_{at}W_{at}$ simulations are indicated
10 in Fig. 5e. Relative to the total response, fixing water vapor concentrations in the radiation code
11 leads to slightly weaker temperature increases in the troposphere and warming throughout the
12 extratropical stratosphere (compare Figs. 5a and 5b). The slightly weaker temperature increases in
13 the $T_{+4K}W_{at}$ simulation are consistent with the facts that 1) temperatures in the T_{+4K} simulation are
14 forced by increases in both surface temperature and the radiative forcing associated with increasing
15 atmospheric emissivity whereas 2) temperatures in the $T_{+4K}W_{at}$ simulation are forced by increases in
16 surface temperature alone.

17 Fixing water vapor concentrations in the radiation code strongly constrains the changes in
18 radiative cooling at the tropopause level and thus the lifting of the regions of largest clear-sky
19 radiative cooling (compare Figs. 5g and 5h). At equilibrium, the changes in clear-sky radiative
20 cooling are predominantly balanced by changes in diabatic heating in cloudy regions. Hence the
21 absence of robust lifting in the isopleths of clear-sky cooling is also reflected in the absence of
22 robust lifting in the clear-sky mass flux divergences (compare Figs. 5j and 5k), cloud fraction
23 (compare Figs. 5m and 5n), and the depth of extratropical wave-driving (compare Figs. 5p and 5q).
24 Interestingly, surface warming appears to account for the poleward shift but not the lifting of the

1 region of largest wave diving (compare Figs. 5p and 5q). The only region where cloud fraction lifts
2 appreciably is at polar latitudes.

3 The right column ($T_{at}W_{+4K}$ minus $T_{at}W_{at}$) shows the response to increasing the water vapor
4 concentrations input into the radiation code to their T_{+4K} values while holding SSTs at their control
5 values. Note that 1) the differences between the specific humidities seen by the radiation code in the
6 $T_{at}W_{-at}$ and $T_{at}W_{at}$ simulations are indicated in Fig. 2d and 2) the specific humidities seen by everything
7 *but* the radiation code in the $T_{at}W_{-at}$ and $T_{at}W_{at}$ simulations are essentially identical and are indicated in
8 Fig. 5f. Increasing the amount of water vapor that the radiation code “sees” has very little effect on
9 the temperature or specific humidity calculated by the dynamical code in the model (Figs. 5c, 5f).
10 This is because: 1) surface temperatures are identical in the $T_{at}W_{at}$ and $T_{at}W_{+4K}$ experiments and 2) the
11 free troposphere of the model is in radiative/convective equilibrium, and thus tropospheric
12 temperatures and saturation specific humidities are likewise nearly identical in the two simulations.
13 The primary differences in temperature between the $T_{at}W_{at}$ and $T_{at}W_{+4K}$ experiments are found in the
14 model stratosphere, where temperatures decrease slightly (Fig. 5c). The decreases in stratospheric
15 temperatures are consistent with 1) increases in the radiative cooling of the stratosphere due to the
16 in-situ increases in water vapor and 2) decreases in the upward radiative flux from the troposphere
17 in regions of the spectrum where the carbon dioxide and water vapor lines overlap.

18 Holding SSTs fixed between the $T_{at}W_{at}$ and $T_{at}W_{+4K}$ experiments provides a strong constraint
19 on the vertical structure of atmospheric temperatures. Hence, the changes in atmospheric cooling
20 rates between the $T_{at}W_{at}$ and $T_{at}W_{+4K}$ experiments arise primarily from changes in the emissivity (due
21 to the differences in water vapor concentrations) and not changes in temperature (i.e., the Planck
22 function). The changes in middle tropospheric clear-sky radiative cooling found in the total response
23 (Fig. 5g) are due primarily to the increases in atmospheric temperatures (Fig. 5h). But the *lifting* of
24 the profiles of clear-sky radiative cooling is due primarily to the increases in water vapor

1 concentrations input into the radiation code (contours in Fig. 5i). Likewise, the lifting in the profiles
2 of clear-sky mass flux divergence, cloud fraction and the EP flux divergence are due mostly to the
3 increases in water vapor concentrations input into the radiation code (compare contours in the
4 bottom three rows of Fig. 5). The largest discrepancies are again found in cloud fraction at polar
5 latitudes, where the increases in clouds are due primarily to the surface warming.

6 The key results from Experiment Sets 2 and 3 are that 1) *locking* the amount of water vapor
7 in the radiation code as SSTs increase leads to a suppression of the lifting of the extratropical
8 tropopause while 2) increasing *only* the amount of water vapor in the radiation code leads to a
9 notable lifting of the extratropical tropopause.

11 *Other experiments*

12 We conducted a series of additional fixed SST aquaplanet experiments that test whether: 1)
13 The absence of stratospheric ozone in the T_{at} and T_{+8K} simulations leads to even smaller changes in
14 tropopause temperature than those indicated in Figs. 2-4 (i.e., ozone contributes to the static stability
15 and thus the amplitude of the clear-sky subsidence in the lower stratosphere; Harrop and Hartmann
16 2012); 2) The results are robust to larger surface warming (increasing SSTs by 8K); and 3) The
17 results are robust to increases in the meridional temperature gradient and thus the potential energy
18 available for conversion to eddy kinetic energy. The results of the additional experiments do not
19 fundamentally change the basic conclusions from this section, and are summarized in the Appendix.

21 **4. Implications for climate change**

22 The results in the previous section suggest that the depth of mixing by extratropical
23 dynamics is constrained by the amplitude of clear-sky radiative cooling by water vapor. The results
24 imply that the extratropical tropopause should remain at roughly the same temperature under

1 climate change. In this section, we explore to what extent this occurs in a climate change simulation
2 run on an AOGCM forced with RCP8.5 scenario emissions.

3 Figure 6 shows meridional profiles of atmospheric temperature and specific humidity from
4 the historical simulation (left) and the differences between the RCP8.5 and historical simulations
5 (right). The differences in atmospheric temperature and specific humidity bear close resemblance to
6 the differences between the control and +4K aquaplanet simulations (compare Figures 2 and 6).
7 Increasing atmospheric greenhouse gases leads to warming throughout the troposphere that peaks in
8 the tropics around 200 hPa, and widespread increases in specific humidity that peak in the lower
9 tropical troposphere. As is the case in the aquaplanet simulations, the 220 K isotherm and 0.5 g/kg
10 isopleth lift by ~ 50 hPa across the globe (black contours).

11 Figure 7 shows attendant results for cloud fraction and the EP flux divergence. As is the case
12 in the aquaplanet GCM response to surface warming, the AOGCM response to RCP8.5 scenario
13 emissions includes a lifting of both cloud fraction and the EP flux divergences throughout the
14 troposphere, as evidenced by the vertical dipoles in the trends in both fields (Figs. 7b, d; shading)
15 and the highlighted isopleths of cloud fraction and EP-flux convergence (Figs. 7b, d; contours). As
16 shown in Figure 8, the cloud top pressure, the level of largest negative EP flux divergence, and the
17 lapse rate tropopause all rise by ~ 50 hPa across the globe in the RCP8.5 scenario (Fig. 8, left column
18 dotted lines), consistent with the upward shift of the tropospheric circulation identified in previous
19 analyses of climate change (Mitchell and Ingram 1992; Santer et al. 2003; Lorenz and DeWeaver
20 2007; Singh and O’Gorman 2012). The key result in Figure 8 is that the temperature of cloud top
21 pressure, largest EP-flux convergence, and the lapse rate tropopause change much less than the
22 temperature on upper tropospheric isobars (Fig. 8, right column).

1 5. Discussion

2 The Clausius-Clapeyron relation leads to a range of “robust” constraints on the atmospheric
3 circulation response to climate change. These include decreases in the convective mass flux (Betts
4 1988; Held and Soden 2006), decreases in the meridional sensible heat transport at midlatitudes
5 (Manabe and Wetherald 1975; Held and Soden 2006), increases in the horizontal moisture flux
6 (Mitchell et al. 1987; Held and Soden 2006), and nearly invariant longwave radiant emissions from
7 tropical anvil clouds (Hartmann and Larson 2002; Zelinka and Hartmann 2010).

8 In a recent study, we argued that the Clausius-Clapeyron relation also leads to a robust
9 constraint on the temperature of the extratropical tropopause and thus the depth of mixing by large-
10 scale extratropical eddies (Thompson et al. 2017). The argument is predicated on the same basic
11 physics that govern anvil cloud temperature in the tropics. That is: The temperature of the
12 tropopause and thus depth of tropospheric mixing should be limited by the amplitude of diabatic
13 sinking motion - and thus radiative cooling - in clear-sky regions not only in the tropics (Hartmann
14 and Larson 2002), but in the extratropics as well. Since clear-sky cooling rates are constrained by
15 water vapor concentrations, diabatic mixing must decrease rapidly at temperatures where the
16 saturation vapor pressure becomes very small.

17 The Clausius-Clapeyron relation may thus be viewed as providing a “thermodynamic
18 constraint” on tropopause temperature and height that acts in conjunction with the “radiative and
19 dynamical constraints” described in Held (1982). The *radiative* constraint defines the tropopause as
20 the lowest level at which the atmosphere is in radiative equilibrium. Hence the tropopause height
21 can be calculated from radiative-convective equilibrium given the tropospheric lapse rate (Held
22 1982). One form of the *dynamical* constraint requires that the tropospheric lapse rate be neutral to
23 both convective and - in the middle latitudes - baroclinic instability (Held 1982; Zurita-Gotor and
24 Lindzen 2007). The *thermodynamic* constraint - as defined here - argues that the extratropical

1 tropopause corresponds to the level where water vapor concentrations (and thus clear-sky radiative
2 cooling) decrease rapidly with height in accordance with the Clausius-Clapeyron relation. The
3 thermodynamic constraint is potentially important, since it implies that extratropical cloud top, the
4 level of largest extratropical wave driving, and the extratropical tropopause should all remain at
5 roughly the same temperature - and thus shift upwards - under climate change. Here we explored
6 the robustness and implications of the constraint in numerical simulations run on an aquaplanet
7 GCM and an AOGCM.

8 We explored three primary sets of simulations run on the aquaplanet GCM: 1) A simulation
9 forced with increases in SSTs; 2) a “locking” simulation forced by increasing SSTs while holding
10 fixed the amount of water vapor input into the radiation code; and 3) a “locking” simulation forced
11 by increasing the amount of water vapor input into the radiation code while holding fixed SSTs. We
12 also explored output from a coupled AOGCM forced with the RCP8.5 emissions scenario. The
13 aquaplanet model response to increasing SSTs and the AOGCM response to increasing greenhouse
14 gases both indicate lifting of the tropospheric circulation under global warming that spans the globe.
15 In the extratropics, the lifting of the circulation is marked by rises in the levels of 1) the largest clear-
16 sky vertical mass flux divergences, 2) cloud top, 3) the largest extratropical wave driving (as given by
17 the EP flux divergence), and 4) the lapse rate tropopause. Importantly, the temperature of all four
18 levels remains roughly invariant even as the surface warms. The aquaplanet locking experiments
19 indicate that 1) locking the amount of water vapor in the radiation code suppresses the lifting of the
20 extratropical tropopause and the deepening of the extratropical tropospheric circulation that occurs
21 in response to surface warming while 2) increasing *only* the amount of water vapor in the radiation
22 code leads to a lifting of the extratropical tropopause and a deepening of the extratropical
23 tropospheric circulation, even when surface temperatures are held fixed. Together, the numerical
24 simulations suggest that 1) longwave radiative cooling - and thus water vapor concentrations -

1 provide a strong constraint on the depth of mixing by large-scale extratropical dynamics; and 2) the
2 temperature of the extratropical tropopause - and thus of extratropical high clouds - remains largely
3 invariant under global warming.

4 The results shown here have several implications for our understanding of the climate
5 system. They suggest that radiative cooling by water vapor plays a central role in governing the
6 vertical structure and amplitude of extratropical dynamics. They suggest that the extratropical
7 tropopause should remain at roughly the same temperature under climate change. They provide a
8 physical explanation for why the extratropical tropospheric circulation should lift in climate change
9 simulations (Mitchell and Ingram 1992; Santer et al. 2003; Lorenz and DeWeaver 2007; Singh and
10 O’Gorman 2012). And they provide a physical explanation for why the positive climate feedbacks
11 associated with high clouds extend throughout much of the globe (Wetherald and Manabe 1988;
12 Zelinka et al. 2012, 2013).

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18 NASA JPL (1439268). This work used the ARCHER UK National Supercomputing Service
19 (<http://www.archer.ac.uk>).

1 **Appendix: Additional experiments**

2 *Increasing SSTs by 4 K with no ozone.* Harrop and Hartmann (2012) argue that cloud top
3 temperatures increase slightly in global warming simulations since a) high clouds penetrate levels
4 where ozone heating contributes to the vertical temperature gradient, and 2) the increases in clear-
5 sky static stability lead to a slight downward shift in the level of largest clear-sky mass fluxes. If the
6 inclusion of stratospheric ozone contributes to increases in cloud top temperature in global-warming
7 simulations, then it follows that cloud-top temperature should be almost perfectly invariant in
8 simulations run without ozone. We redid the T_{+4K} and T_{cl} simulations after setting the concentrations
9 of all radiatively active gases other than water vapor to effectively zero (i.e., $T_{+4K, no}$ and $T_{cl, no}$). The
10 experiments are similar to the “H2Oonly” experiments in Harrop and Hartmann (2012), except that
11 their runs are performed on a cloud resolving model and ours are performed in a GCM.

12 The heights of the model lapse-rate tropopause and the largest clear-sky mass flux
13 divergences are largely unchanged across the globe between the $T_{cl, no}$ and T_{cl} simulations, consistent
14 with our hypothesis that the global tropopause is governed primarily by the vertical structure of
15 water vapor radiative cooling (not shown). However, removing ozone and carbon dioxide also leads
16 to clouds that extend to temperatures below 190 K and thus well above the 50 hPa level in the
17 tropics in the $T_{cl, no}$ simulation (see also Harrop and Hartmann 2012, Fig. 5). The extension of clouds
18 to 190 K is consistent with the decreases in stratospheric static stability and temperature that
19 accompany the removal of ozone (Harrop and Hartmann 2012). Consistent with Harrop and
20 Hartmann (2012, Fig. 6), cloud top temperatures are effectively invariant between the $T_{+4K, no}$ and $T_{cl, no}$
21 simulations, even though they extend to higher levels in both simulations.

22 *Increasing SSTs by 8 K.* Simulations run in an identical manner to T_{+4K} but for SST raised by 8
23 K yield very similar conclusions to those derived from the T_{+4K} simulation. The isopleths of upper
24 tropospheric clear-sky radiative cooling, cloud top pressure, the level of largest EP flux divergences

1 and the lapse-rate tropopause all lift by roughly twice as much as they do in the T_{+4K} simulation.
2 Cloud top temperature remains nearly invariant at extratropical latitudes, but increases slightly in the
3 tropics consistent with the accompanying increases in clear-sky static stability. The increases in static
4 stability mean that a smaller clear-sky mass flux is required to balance a given diabatic heating, and
5 arise from 1) the shift in tropospheric temperatures to warmer moist adiabats (Zelinka and
6 Hartmann 2010); and 2) the extension of cloud top to altitudes where ozone heating contributes to
7 the vertical temperature gradient (Harrop and Hartmann 2012).

8 *Increasing the meridional temperature gradient by 2 K and 4 K.* The default SST distribution has two
9 parameters for the maximum and minimum SST. In the Qobs distribution used in the T_{at} simulation,
10 these are 27°C and 0°C (see Neale and Hoskins 2000 for details of the distribution). We ran two
11 experiments where the maximum and minimum SST were changed to [28°C and -1°C] and [29°C
12 and -2°C], thus increasing the equator-to-pole temperature gradient by 2 K and 4 K, respectively.
13 Increasing the meridional temperature gradient provides additional potential energy for developing
14 baroclinic waves and scales with the meridional slope and height of the extratropical tropopause
15 (e.g., Stone 1978; Schneider 2004). It also increases the strength of the westerly flow in the upper
16 troposphere/lower stratosphere, thus allowing a larger spectrum of zonal wavenumbers to
17 propagate vertically into the model stratosphere. A strengthening of the model Brewer-Dobson
18 circulation would be expected to lead to a lifting of the tropopause in the tropics and depression of
19 the tropopause at high latitudes (e.g., Thuburn and Craig 2000; Birner 2010; Haqq-Misra et al 2011)
20 but - according to our hypothesis - little change in tropopause temperatures.

21 The most pronounced differences in the extratropical circulation when the meridional temperature
22 gradient is increased include a lifting of extratropical clouds to slightly lower pressures and less EP
23 flux convergence in the extratropical upper troposphere (the reasons for the weakening of the wave-
24 driving are unclear but are not the focus of this study). The isopleths of extratropical clear-sky

- 1 radiative cooling, cloud top pressure, largest mass flux divergence, largest EP flux convergence and
- 2 the lapse-rate tropopause all remain at roughly the same temperature across the globe when the
- 3 meridional temperature gradient is increased by both 2 K and 4 K.

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Figure Captions

Figure 1. The annual-mean, long term-mean (shading) EP flux divergence and (contours) Lagrangian-mean TEM circulation. Results are derived from ERA Interim. The EP flux divergence is multiplied by the cosine of latitude. Contour intervals are at 8×10^{-9} kg/s (1000-200hPa), 4×10^{-9} kg/s (200-100hPa), 2×10^{-9} kg/s (100-50hPa), 1×10^{-9} kg/s (50-25hPa), and 0.5×10^{-9} kg/s (25-10hPa).

Figure 2. The long-term mean, zonal-mean temperature (top) and specific humidity (bottom) from the T_{at} simulation (left) and the difference between T_{+4K} and T_{at} simulations (right). The black contours indicate the 220 K (top) and 0.05 g/kg (bottom) isopleths from the T_{at} (solid) and T_{+4K} (dashed) simulations. Note that specific humidity is plotted on a logarithmic scale since water vapor concentrations decrease exponentially with height.

Figure 3. The long-term mean, zonal-mean clear-sky radiative cooling, mass flux divergence, cloud fraction, and EP flux divergence from the T_{at} simulation (left) and the difference between T_{+4K} and T_{at} simulations (right). The black contours indicate isopleths from the (solid) T_{at} and (dashed) T_{+4K} simulations of: (a, b) -0.5 K/day, (c, d) the level of largest mass flux divergence, (e, f) cloud fraction of 0.07, and (g, h) the -5 m/s/day EP flux convergence contour. The EP flux divergence is multiplied by the cosine of latitude.

Figure 4. Left: The long-term mean, zonal-mean 220 K isotherm (solid lines all panels) overlaid with the mass flux divergence maximum (dotted line in panel a), cloud top (dotted line in panel c), the level of maximum EP flux convergence (dotted line in panel e), and the lapse-rate tropopause (dotted line in panel g). Black denotes results from the T_{at} simulation; red from the T_{+4K} simulation.

1 **Right:** As in the left panel, but results are plotted as a function of temperature, and the 220 K
2 isotherm is replaced with the temperature at the 300 hPa level. Cloud top pressure (temperature) is
3 found as the average pressure (temperature) over the top three model layers where cloud fraction >
4 0.01.

5
6 **Figure 5.** Rows show the differences between the (left) T_{+4K} and T_{at} simulations; (middle) $T_{+4K}W_{at}$ and
7 $T_{at}W_{at}$ simulations; and (right) $T_{at}W_{+4K}$ and $T_{at}W_{at}$ simulations. Rows show results for (from top to
8 bottom) zonal-mean temperature; specific humidity; clear-sky radiative cooling; clear-sky mass flux
9 divergence; cloud fraction, and the EP flux divergence. The black contours indicate the isopleths of
10 (a) 220 K, (b) 0.05 g/kg, (c) -0.5 K/day, (d) the level of largest mass flux divergence, (e) cloud
11 fraction of 0.07 and (f) the -5 m/s/day EP flux convergence contours from the $T_{at}W_{at}$ (solid in all
12 columns) and T_{+4K} (dashed in left column), $T_{+4K}W_{at}$ (dashed in middle column), and $T_{at}W_{+4K}$ (dashed in
13 right column) simulations. The EP flux divergence is multiplied by the cosine of latitude. The results
14 in the left panel are reproduced from the right columns in Figs. 2 and 3.

15
16 **Figure 6.** As in Figure 2, but for temperature and specific humidity from the historical simulation
17 (left) and the differences between the RCP8.5 and historical simulations (right). The historical
18 simulation is averaged 1979-2005; the RCP8.5 simulation is averaged between 2070-2099. The solid
19 black contours indicate the 220 K (left) and 0.05 g/kg (right) isopleths from the historical (solid) and
20 RCP8.5 (dashed) simulations. Output is from the CMIP5 simulations run on the IPSL-CM5A-LR
21 climate model.

22
23 **Figure 7.** As in the bottom two rows of Figure 3, but for cloud fraction and the EP flux divergence
24 from the historical simulation (left) and the differences between the RCP8.5 and historical

1 simulations (right). The black contours indicate where cloud fraction equals 0.07 (top) and the EP
2 flux divergence equals -2.5 m/s/day (bottom) from the historical (solid) and RCP8.5 (dashed)
3 simulations. Output is from the CMIP5 simulations run on the IPSL-CM5A-LR climate model. The
4 EP flux divergence is multiplied by the cosine of latitude.

5

6 **Figure 8.** As in the bottom three rows of Figure 4, but for results from the historical (black) and
7 RCP8.5 (red) simulations. Output is from the CMIP5 simulations run on the IPSL-CM5A-LR
8 climate model.

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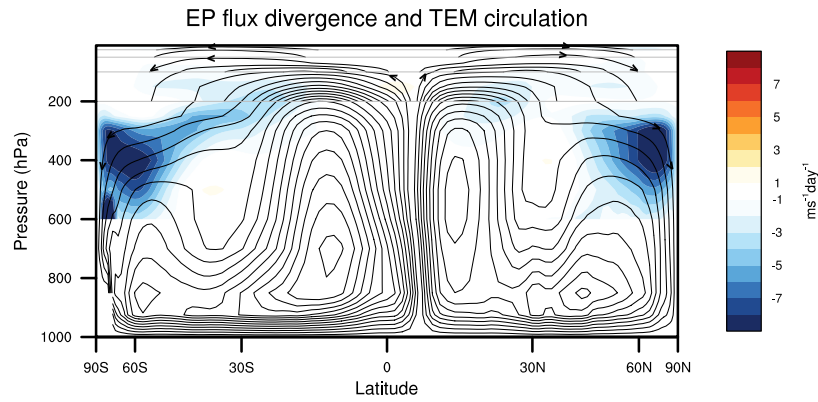
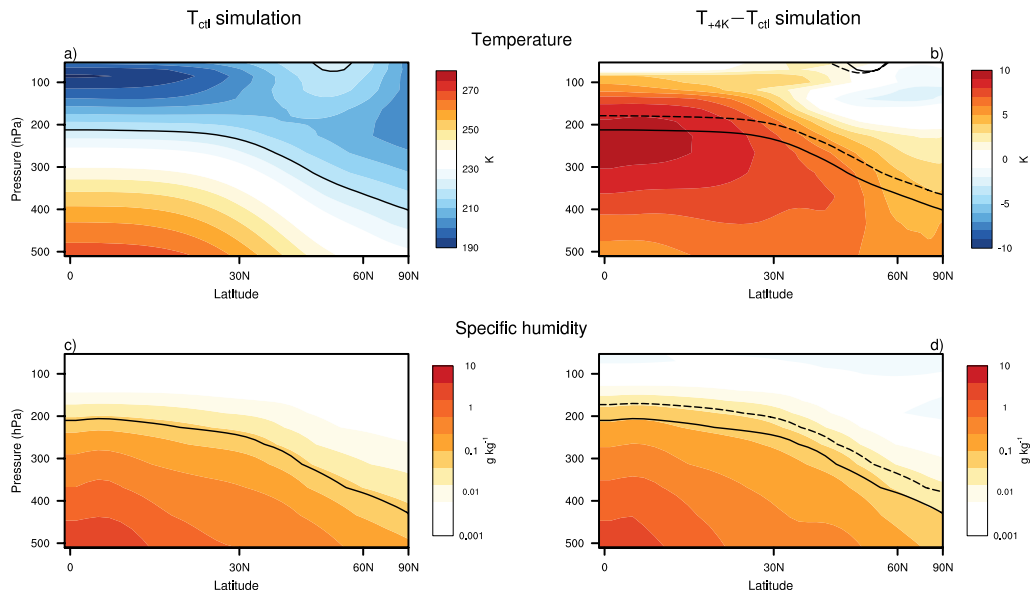


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Figure 2. The long-term mean, zonal-mean temperature (top) and specific humidity (bottom) from the T_{cil} simulation (left) and the difference between T_{+4K} and T_{cil} simulations (right). The black contours indicate the 220 K (top) and 0.05 g/kg (bottom) isopleths from the T_{cil} (solid) and T_{+4K} (dashed) simulations. Note that specific humidity is plotted on a logarithmic scale since water vapor concentrations decrease exponentially with height.

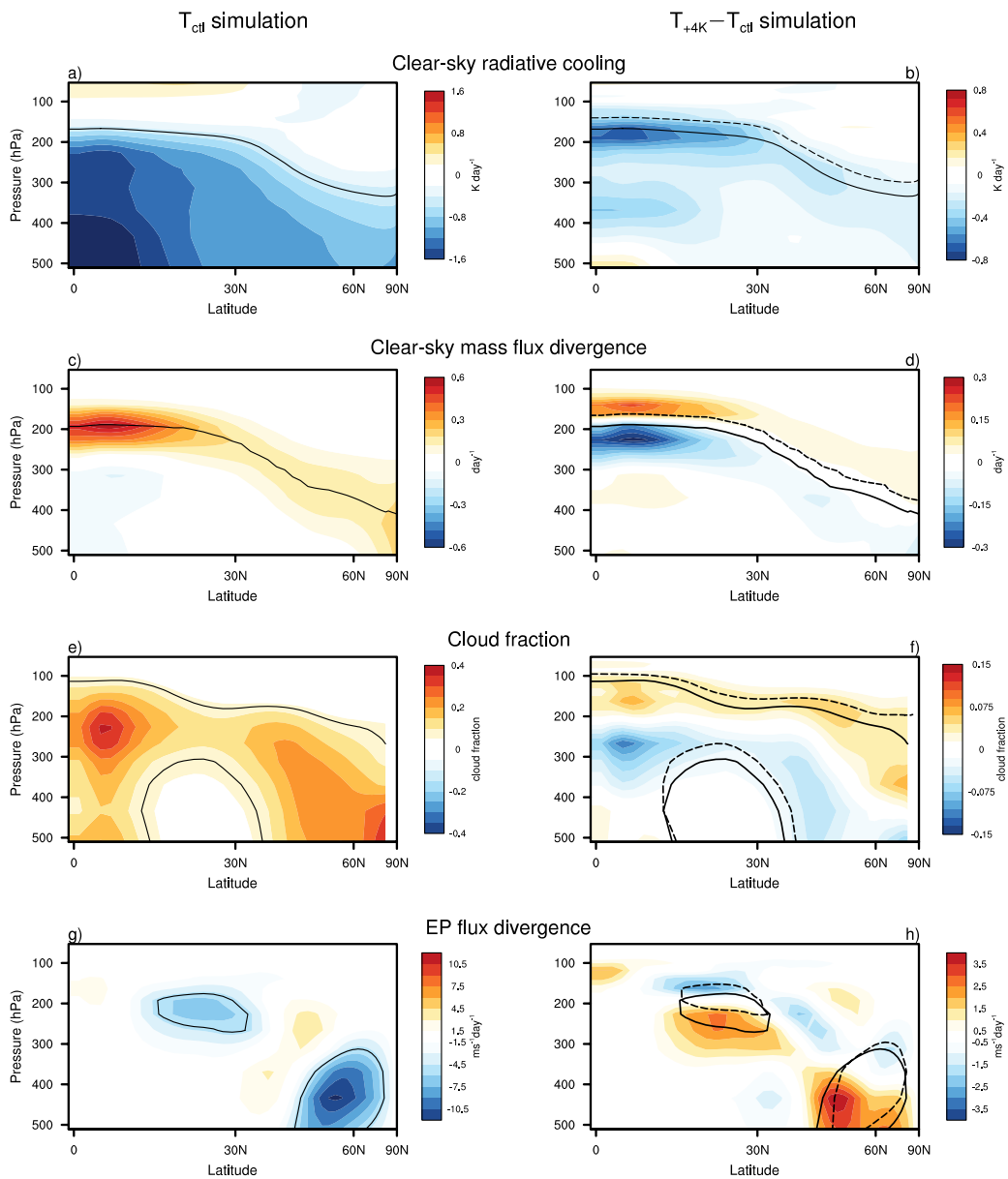
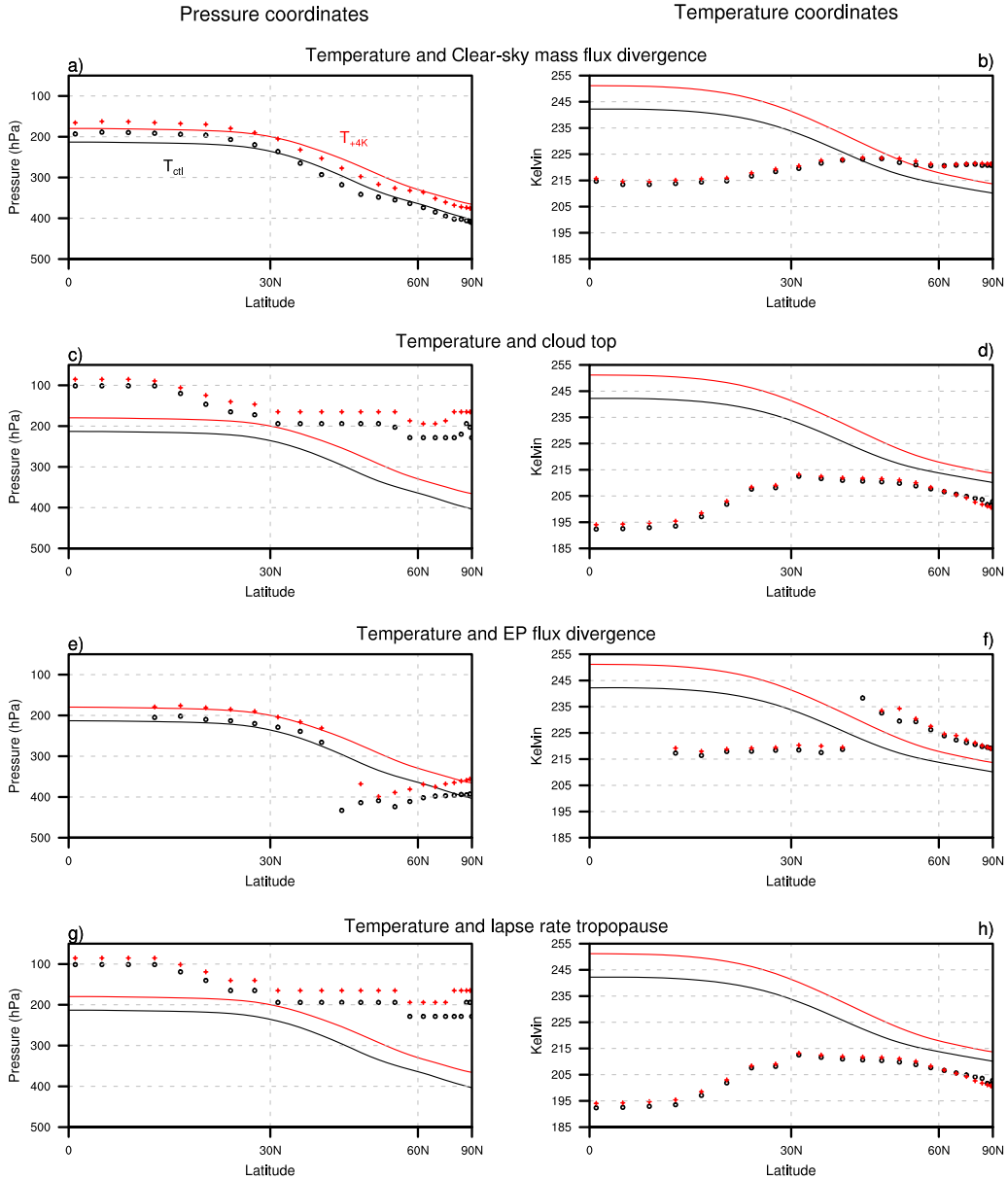


Figure 3. The long-term mean, zonal-mean clear-sky radiative cooling, mass flux divergence, cloud fraction, and EP flux divergence from the T_{ctl} simulation (left) and the difference between T_{+4K} and T_{ctl} simulations (right). The black contours indicate isopleths from the (solid) T_{ctl} and (dashed) T_{+4K} simulations of: (a, b) -0.5 K/day, (c, d) the level of largest mass flux divergence, (e, f) cloud fraction of 0.07, and (g, h) the -5 m/s/day EP flux convergence contour. The EP flux divergence is multiplied by the cosine of latitude.



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Figure 4. **Left:** The long-term mean, zonal-mean 220 K isotherm (solid lines all panels) overlaid ² with the mass flux divergence maximum (dotted line in panel a), ³ cloud top (dotted line in panel c), the level of maximum EP flux convergence (dotted line in panel e), and the lapse-rate tropopause (dotted line in panel g). Black denotes results from the T_{cil} simulation; red from the T_{+4K} simulation. **Right:** As in the left panel, but results are plotted as a function of temperature, and the 220 K isotherm is replaced with the temperature at the 300 hPa level. Cloud top pressure (temperature) is found as the average pressure (temperature) over the top three model layers where cloud fraction > 0.01.

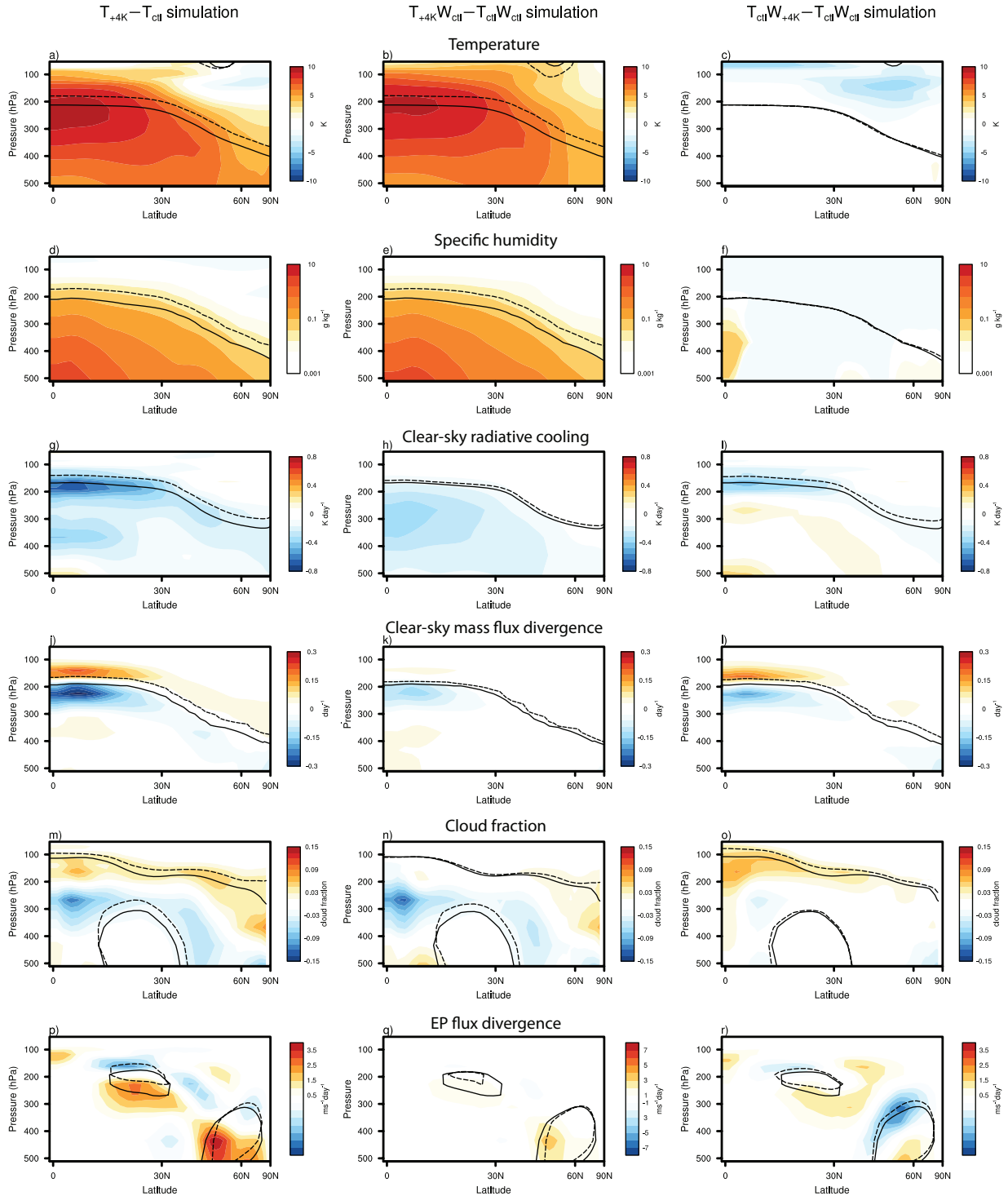
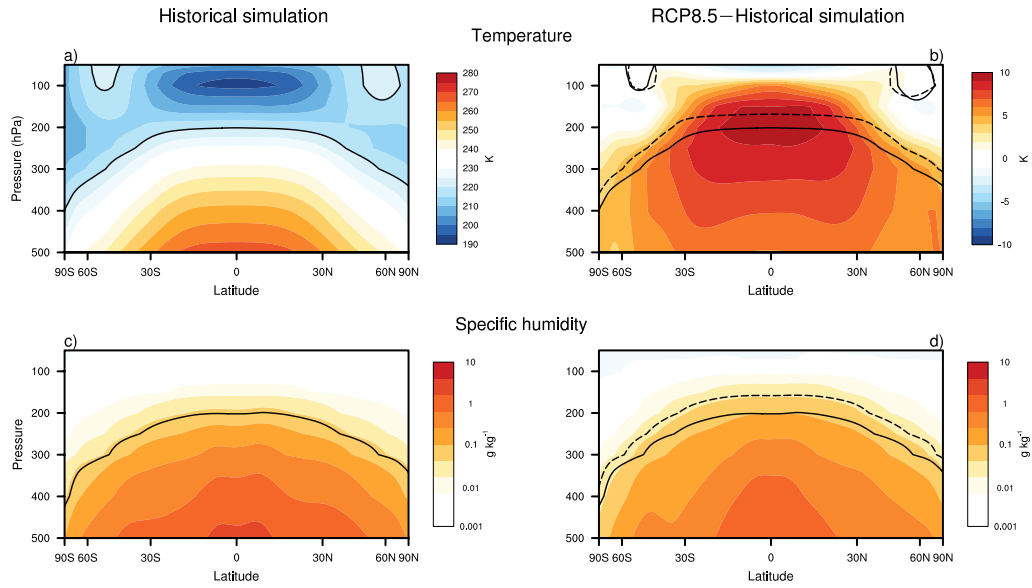


Figure 5. Rows show the differences between the (left) T_{+4K} and T_{ctl} simulations; (middle) $T_{+4K}W_{ctl}$ and $T_{ctl}W_{ctl}$ simulations; and (right) $T_{ctl}W_{+4K}$ and $T_{ctl}W_{ctl}$ simulations. Rows show results for (from top to bottom) zonal-mean temperature; specific humidity; clear-sky radiative cooling; clear-sky mass flux divergence; cloud fraction, and the EP flux divergence. The black contours indicate the isopleths of (a) 220 K, (b) 0.05 g/kg, (c) -0.5 K/day, (d) the level of largest mass flux divergence, (e) cloud fraction of 0.07 and (f) the -5 m/s/day EP flux convergence contours from the $T_{ctl}W_{ctl}$ (solid in all columns) and T_{+4K} (dashed in left column), $T_{+4K}W_{ctl}$ (dashed in middle column), and $T_{ctl}W_{+4K}$ (dashed in right column) simulations. The EP flux divergence is multiplied by the cosine of latitude. The results in the left panel are reproduced from the right columns in Figs. 2 and 3.

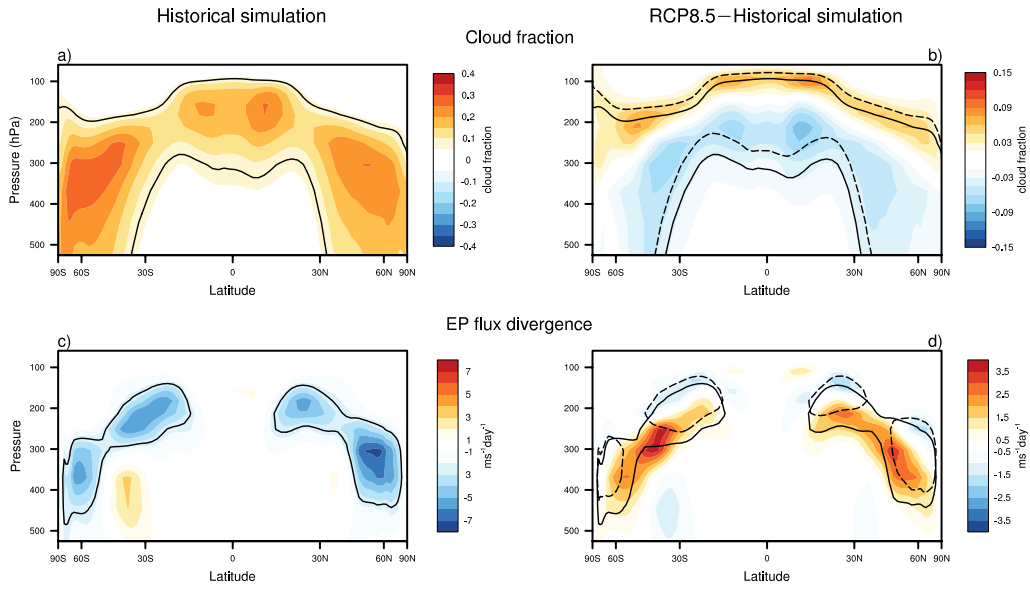
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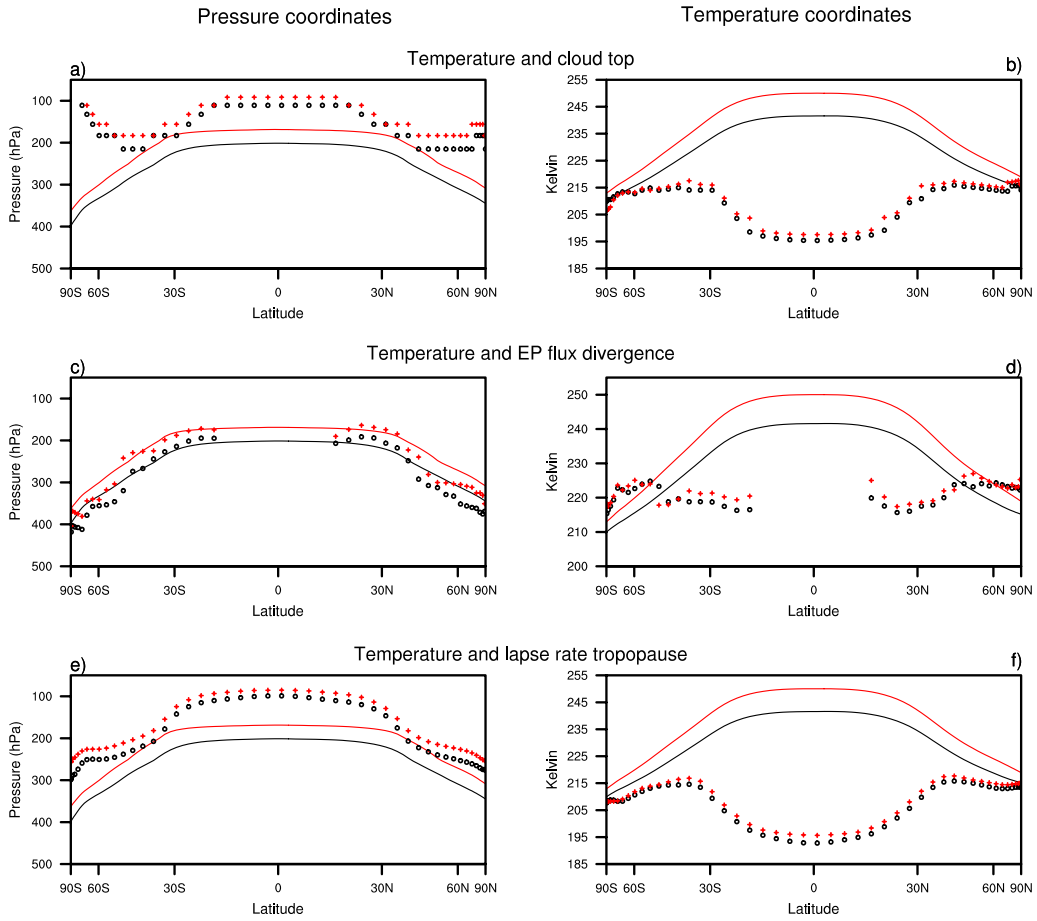
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Figure 7. As in the bottom two rows of Figure 3, but for cloud fraction and the EP flux divergence from the historical simulation (left) and the differences between the RCP8.5 and historical simulations (right). The black contours indicate where cloud fraction equals 0.07 (top) and the EP flux divergence equals -2.5 m/s/day (bottom) from the historical (solid) and RCP8.5 (dashed) simulations. Output is from the CMIP5 simulations run on the IPSL-CM5A-LR climate model. The EP flux divergence is multiplied by the cosine of latitude.



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Figure 8. As in the bottom three rows of Figure 4, but for results from the historical (black) and RCP8.5 (red) simulations. Output is from the CMIP5 simulations run on the IPSL-CM5A-LR climate model.